

$$g(x) = mx \quad m > 0 \quad \text{Schnittpunkt } z(z=f(x))$$

$$\begin{aligned} A_1 &= \int_0^2 (f(x) - g(x)) dx \\ &= \int_0^2 (3 \sin\left(\frac{\pi}{4}x\right) - mx) dx \\ &= \left[ -\frac{12}{\pi} \cos\left(\frac{\pi}{4}x\right) - \frac{m}{2}x^2 \right]_0^2 \\ &= \left[ -\frac{12}{\pi} \cos\left(\frac{\pi \cdot 2}{4}\right) - \frac{m \cdot 2^2}{2} \right] - \left[ -\frac{12}{\pi} \cos(0) \right] \\ &= -\frac{12}{\pi} \cos\left(\frac{\pi \cdot 2}{4}\right) - \frac{m \cdot 2^2}{2} + \frac{12}{\pi} \end{aligned}$$

$$\begin{aligned} A_2 &= \int_2^4 (g(x) - f(x)) dx \\ &= \int_2^4 (mx - 3 \sin\left(\frac{\pi}{4}x\right)) dx \\ &= \left[ \frac{m}{2}x^2 + \frac{12}{\pi} \cos\left(\frac{\pi}{4}x\right) \right]_2^4 \\ &= \left[ 8m + \frac{12}{\pi} \cos(\pi) \right] - \left[ \frac{m \cdot 2^2}{2} + \frac{12}{\pi} \cos\left(\frac{\pi}{4} \cdot 2\right) \right] \\ &= 8m - \frac{12}{\pi} - \frac{m \cdot 2^2}{2} - \frac{12}{\pi} \cos\left(\frac{\pi \cdot 2}{4}\right) \end{aligned}$$

$$A_1 = A_2$$
$$-\frac{12}{\pi} \cos\left(\frac{\pi \cdot 2}{4}\right) - \frac{m \cdot 2^2}{2} + \frac{12}{\pi} = 8m - \frac{12}{\pi} - \frac{m \cdot 2^2}{2} - \frac{12}{\pi} \cos\left(\frac{\pi \cdot 2}{4}\right)$$

$$-\frac{12}{\pi} \cos\left(\frac{\pi \cdot 2}{4}\right) + \frac{12}{\pi} = 8m - \frac{12}{\pi} - \frac{12}{\pi} \cos\left(\frac{\pi \cdot 2}{4}\right)$$

$$\frac{12}{\pi} = 8m - \frac{12}{\pi}$$

$$8m = \frac{24}{\pi}$$

$$m = \frac{3}{\pi}$$

$$m \approx 0,95$$